## **VCU Discrete Mathematics Seminar**

## 3-Bootstrap Percolation on Grids and Tori

## Prof Neal Bushaw (VCU!)

Wednesday, Oct. 22 1:00-1:50 EDT

**In person** in 4145 Harris Hall. And a Zoom option:

https://vcu.zoom.us/j/81475528886 password=graphs2357



At each step of the k-neighbor bootstrap percolation process on a graph, every uninfected vertex with at least k infected neighbors becomes infected. An initial set of infected vertices PERCOLATES if eventually every vertex becomes infected. Determining the minimum size of a percolating set under the 2-bootstrap model is a classic combinatorial puzzle – the slower infection of the 3-bootstrap process seems harder to analyze. Building on the work of Dukes, Noel, and Romer, we determine precisely the minimum size of a percolating in an  $(m \times n)$  grid. We then consider the same question for toroidal grid graphs.

This is joint work with Alexander Clifton.

For the DM seminar schedule, see:

https://go.vcu.edu/discrete